

# Syllabus for SUTD 40.616 (Fall 2025)

## “Special Topics in Games, Learning, and Optimization”

### 1 General Information

**Course Description:** This is a graduate-level theory course providing a modern treatment of *online learning* and *learning in games*. The course is centered on the online learning framework as a paradigm for sequential decision making within strategic and non-stationary environments. Particular attention will be devoted to showing how online learning dynamics lead to equilibria in multi-agent, game-theoretic settings.

The course is designed for students interested in algorithmic game theory, multi-agent learning and optimization. Lectures will introduce the online learning paradigm, fundamental algorithms, key results, and analysis techniques, with the aim of preparing students to pursue research in this area.

**Instructors:** Anas Barakat, John Lazarsfeld, and Joseph Sakos (*Postdoctoral Research Fellows in ESD Pillar*)

**Time:** Tuesdays and Thursdays, 10am-12pm SGT (*starting on 2025.09.16*)

**Location:** SUTD Think Tank 11

**Contact email:** [sutd.glo.course@gmail.com](mailto:sutd.glo.course@gmail.com)

**Prerequisites:** Prior courses in calculus, linear algebra, and basic notions of probability and analysis. A prior course in optimization is helpful but not absolutely necessary. Prior knowledge of game theory is not required.

### 2 Overview of Topics

The course will consist of twice-weekly lectures organized in four parts – Part I: Online Learning, Part II: Learning in Normal-Form and Stochastic Games, Part III: Learning in Extensive-Form and Continuous Games, Part IV: Special Topics. A tentative schedule of lecture topics is as follows:

#### Part I: Online Learning – Lectures given by John

- (Lo1) – [Introduction to Online Learning](#)  
*Prediction with expert advice, online convex optimization, regret, Multiplicative Weights Update and Online Gradient Descent.*
- (Lo2) – [Follow-the-Regularized-Leader: No-regret via Regularization](#)  
*Family of leader-based algorithms, analysis of Follow-the-Regularized-Leader (FTRL) via coupling with Be-the-Leader/Follow-the-Leader, Multiplicative Weights Update as FTRL, lower bounds for online learning.*
- (Lo3) – [Follow-the-Perturbed-Leader and Online Mirror Descent: No-regret via Perturbation and Penalty](#)  
*Follow-the-Perturbed-Leader (FTPL) analysis, equivalence between FTPL and FTRL, Online Mirror Descent analysis.*
- (Lo4) – [Online Learning with Bandit Feedback](#)  
*Bandit feedback model, expected regret and pseudo-regret, EXP3 algorithm for adversarial bandits, Explore-then-Commit and UCB algorithms for stochastic bandits.*
- (Lo5) – [Φ-Regret Minimization](#)  
*Beyond external regret: swap-regret, internal-regret, and Φ-regret framework. Blum-Mansour and Stoltz-Lugosi algorithms.*
- (Lo6) – [Blackwell Approachability and Regret Matching](#)  
*Blackwell’s Approachability theorem, Regret Matching (RM) and Regret Matching+ (RM+) algorithms.*

#### Part II: Learning in Normal-Form and Stochastic Games – Lectures given by Anas

- (Lo7) – [Introduction to Normal-Form Games and Nash Equilibria](#)  
*Normal-form games, Nash equilibria (NE), game classes (potential, zero-sum, decomposition).*
- (Lo8) – [No-Regret Learning in Games and Learning NEs in Zero-Sum and Potential Games](#)  
*Hindsight rationality, proof of minimax theorem via online learning, learning NE in potential games.*
- (Lo9) – [Learning \(Coarse\)-Correlated Equilibria in General-Sum Games](#)  
*(Coarse)-correlated equilibria, time-average convergence via no-φ-regret learning, average vs. last-iterate convergence.*
- (L10) – [Optimistic Learning and Social Welfare of No-Regret Dynamics](#)  
*Optimistic FTRL algorithms, RVU bounds, individual vs. sum of regrets, fast convergence of social welfare.*
- (L11) – [Introduction to Stochastic Games and Multi-Agent Reinforcement Learning](#)  
*Introduction to Markov Decision Processes (MDPs) and Reinforcement Learning, definition of stochastic games, Shapley’s minimax theorem, existence of Nash equilibria.*
- (L12) – [Learning Equilibria in Stochastic Games](#)  
*Independent and decentralized learning, zero-sum Markov games and Markov potential games, policy gradient methods.*

**Part III: Learning in Extensive-Form and Continuous Games** – Lectures given by Joseph

- (L13) – [Introduction to Extensive-Form Games](#)  
*Game trees, imperfect information, perfect recall, strategy representations, Kuhn's theorem.*
- (L14) – [Learning Equilibria in Extensive-Form Games](#)  
*Counterfactual Regret Minimization (CFR) algorithm and speedups.*
- (L15) – [Introduction to Continuous Games](#)  
*Concave games, Rosen's theorem, variational inequalities, monotone games, zero-sum games and Gradient Descent Ascent (GDA), divergence of GDA in bilinear case.*
- (L16) – [Learning Equilibria in Continuous Games](#)  
*Proximal point method, Optimistic GDA and Extragradient algorithms for zero-sum games, learning equilibria in potential games, general concave games.*
- (L17) – [Price of Anarchy and Equilibrium Selection](#)  
*Braess's paradox, Pigou's network, smooth games, introduction to Price of Anarchy (PoA) bounds.*

**Part IV: Special Topics**

The final six lectures will cover more advanced topics based on results in the field over the past five years:

- (L18) – [Online Learning in Time-Varying Games](#) (Anas)
- (L19) – [\(Multi-Agent\) Online Nonstochastic Control](#) (Anas)
- (L20) – [Bridging Continuous-time and Discrete-time Learning in Games](#) (John)
- (L21) – [Unregularized Learning in Zero-Sum Games](#) (John)
- (L22) – [Sum-of-Squares Optimization in Games](#) (Joseph)
- (L23) – [Hidden Games](#) (Joseph)

**3 Assignments and Final Project**

The course will involve two problem sets and a final project.

**Homeworks:** Each problem set will consist of several exercises based on topics covered in the lectures.

- *Problem Set A:* released Friday, 2025.09.18; due Friday, 2025.10.10.
- *Problem Set B:* released Friday, 2025.10.17; due Friday, 2025.11.14.

**Final Project:** Students will perform a final project based on reading and synthesizing several related papers about an active research area in the field. The instructors will propose a list of projects with a list of papers and will match students with topics based on interest. Students will give a short midterm presentation on their topics, prepare a final report, and give a final presentation in the last week of the course.

- *Project topic preference rankings:* due Friday, 2025.10.03.
- *Midterm presentations and feedback:* Tuesday, 2025.11.04. (5-10 minutes per student).
- *Final presentations:* Tuesday, 2025.12.16 and Thursday, 2025.12.18. (15-20 minutes per student).
- *Final report:* due Friday, 2025.12.19.

**Grading:** Will be based on the following percentages:

- **Homework:** 40% (20% per assignment)
- **Final Project:** 60% (midterm presentation: 10%, final presentation: 20%, final report: 30%).

*More details on problem sets and final project will be covered in the first two lectures of the course.*

**4 References and Resources**

Lecture notes and/or slides will be posted before each class. The content of the lectures draws from a variety of (both classical and modern) references, including the following texts:

- Cesa-Bianchi and Lugosi, 2006. *Prediction, Learning, and Games.*
- Hazan, 2016. *Introduction to Online Convex Optimization.*
- Nisan, Roughgarden, Tardos, and Vazirani, 2007. *Algorithmic Game Theory.*
- Orabona, 2019. *A Modern Introduction to Online Learning.*

*Additional references and pointers will be given throughout the course.*